

AD

RSIC-686

THE PRINCIPAL FACTORS DETERMINING THE DIRECTIONAL
PATTERN OF A DIELECTRIC ANTENNA

by

G. Zh. Rankis

Izvestiya VUZOV SSSR - Radiotekhnika (Radio Engineering),

Vol. IX, No. 1, 1966, pp. 97-104

Translated from the Russian

July 1967

DISTRIBUTION UNLIMITED

REDSTONE SCIENTIFIC INFORMATION CENTER
REDSTONE ARSENAL, ALABAMA

JOINTLY SUPPORTED BY



U.S. ARMY MISSILE COMMAND



GEORGE C. MARSHALL SPACE FLIGHT CENTER

N67-37491

FACILITY FORM 602

(ACCESSION NUMBER)

12

(PAGES)

~~CR-88645~~

(NASA CR OR TMX OR AD NUMBER)

TMX-60335

(THRU)

(CODE)

(CATEGORY)

Disclaimer

The findings in this report are not to be construed as an official Department of the Army position unless so designated by other authorized documents.

Disposition

Destroy this report when it is no longer needed. Do not return it to the originator.

RSIC-686

THE PRINCIPAL FACTORS DETERMINING THE DIRECTIONAL
PATTERN OF A DIELECTRIC ANTENNA

by

G. Zh. Rankis

Izvestiya VUZOV SSSR - Radiotekhnika (Radio Engineering),

Vol. IX, No. 1, 1966, pp. 97-104

Translated from the Russian

July 1967

DISTRIBUTION UNLIMITED

REDSTONE SCIENTIFIC INFORMATION CENTER
REDSTONE ARSENAL, ALABAMA

JOINTLY SUPPORTED BY

**U.S. ARMY MISSILE COMMAND****GEORGE C. MARSHALL SPACE FLIGHT CENTER**

77 37491

FACILITY FORM 602

(ACCESSION NUMBER)

(THRU)

(PAGES)

(CODE)

NASA CR OR TMX OR AD NUMBER

(CATEGORY)

3 July 1967

RSIC-686

THE PRINCIPAL FACTORS DETERMINING THE DIRECTIONAL
PATTERN OF A DIELECTRIC ANTENNA

by

G. Zh. Rankis

Izvestiya VUZOV SSSR - Radiotekhnika (Radio Engineering) ,

Vol. IX, No. 1, 1966, pp. 97-104

Translated from the Russian

DISTRIBUTION UNLIMITED

Translation Branch
Redstone Scientific Information Center
Research and Development Directorate
U. S. Army Missile Command
Redstone Arsenal, Alabama 35809

The directional pattern of a dielectric antenna is analyzed on the basis of integral equations. Additional factors are established which determine the difference of the directivity pattern of a real antenna from an idealized linear travelling-wave antenna: direct radiation of the exciting junction, a supplementary field in the region of the exciting junction, etc. Estimates of the magnitude of their influence were obtained for different varieties of dielectric antennas. The properties of conical dielectric antennas are briefly examined.

The basic idea of the theory and method of engineering calculation of dielectric antennas at the present time is the concept of the characteristic wave of an infinite dielectric waveguide as the main factor determining its directional pattern. Such a concept, in spite of extreme idealization of the actual conditions, at least explains the main features of the radiation pattern. Because of the physical simplicity and clarity of that model it is of interest to construct on the basis of it a more precise theory of a dielectric antenna. The purpose of the present work is to explain the main factors whose effect leads to deviation of the directional pattern of a real antenna from the idealized model. From that point of view the model can be considered a first approximation which will be refined later with consideration of other factors. The advisability of such an examination is confirmed still more by the fact that rigorous problems of the diffractive excitation of dielectric waveguides in the three-dimensional case have not been solved.

An Expression for the Directional Pattern

Let us examine a dielectric antenna protruding from an infinite plane ideally conducting screen (Figure 1). By applying the method of functions of elementary sources a system of integral equations can be derived for the field intensity.¹

$$\begin{aligned} [\vec{E}(\mathbf{r}), \vec{a}] - j\omega \int_V [\epsilon(\mathbf{r}') - \epsilon_0] [\vec{E}(\mathbf{r}'), \vec{E}_1(\mathbf{r}, \mathbf{r}')] dV' \\ = - \int_{S_0} \{ [\vec{E}(\mathbf{r}'), \vec{H}_1(\mathbf{r}, \mathbf{r}')] , \vec{dS}' \} , \end{aligned} \quad (1)$$

where $\vec{E}(\mathbf{r})$ is the field at the point of observation M, the set of coordinates of which we will designate by \mathbf{r} , $\vec{E}_1(\mathbf{r}, \mathbf{r}')$; $\vec{H}_1(\mathbf{r}, \mathbf{r}')$ is the field of an elementary vibrator located at the point M in the direction \vec{a} at the current point of the antenna \mathbf{r}' ; $\epsilon(\mathbf{r}')$ is the distribution function of the dielectric constant over the volume of the antenna; $\vec{E}_\tau(\mathbf{r}')$ is the field in the exciting aperture ($z = 0$).

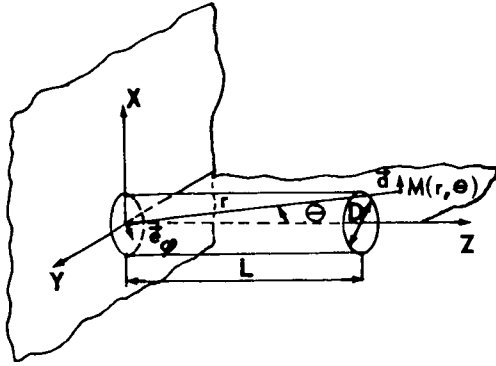


Figure 1

The single vector \vec{a} can be expanded in three mutually perpendicular directions; therefore Eq. (1) decomposes into three scalar equations.

If the field within the dielectric and at S_0 is known, then a formula for calculation of the field created by the dielectric antenna follows from Eq. (1). For an antenna uniform in length and occupying the volume V_0 it assumes the form

$$[\vec{E}(\mathbf{r}), \vec{a}] = j\omega(\epsilon - \epsilon_0) \int_{V_0} [\vec{E}(\mathbf{r}'), \vec{E}_1(\mathbf{r}, \mathbf{r}')] dV' - \int_{S_0} \{ [\vec{E}_T(\mathbf{r}'), \vec{H}_1(\mathbf{r}, \mathbf{r}')] , d\vec{S} \}. \quad (2)$$

We will use that formula to investigate the directional pattern. Let the plane XZ be E, the plane of the antenna. Let us examine the directivity pattern of the field of major polarization in the plane H(YZ). Then \vec{a} must be directed parallel to the X-axis.

We will represent the field within the antenna in the form

$$\vec{E}(\mathbf{r}') = \vec{E}_0(\mathbf{r}') + \vec{E}'(\mathbf{r}'), \quad (3)$$

where $\vec{E}_0(\mathbf{r}')$ is the field of the characteristic wave of the dielectric waveguide, and $\vec{E}'(\mathbf{r}') = \vec{E}(\mathbf{r}') - \vec{E}_0(\mathbf{r}')$ is the difference between the real field in the antenna and the field of the characteristic wave. We will call that difference the supplementary field. The field of the characteristic wave can be represented in the form

$$\vec{E}_0(\mathbf{r}') = \vec{E}_0(x, y) e^{-jk_d z} e^{j\psi}.$$

With consideration of (3) and (4), expression (2) gives

$$E_a(x, y, z) = j\omega(\epsilon - \epsilon_0) e^{j\psi} \int_0^L e^{-jk_d z'} dz' \int_{S_T} [\vec{E}_0(x'; y'), \vec{E}_1(x, y, z; x', y', z')] dx' dy'$$

$$\begin{aligned}
& + j\omega (\epsilon - \epsilon_0) \int_{V_0} [\vec{E}'(x', y'), \vec{E}_1(x, y, z; x', y', z')] dx' dy' dz' \\
& - \int_{S_0} \{ [\vec{E}_\tau(x', y'), \vec{H}_1(x, y, z; x', y', z')] \cdot d\vec{S}' \}.
\end{aligned} \tag{4}$$

Here the field intensity at the point of observation is represented as the sum of three components: the field created by the characteristic wave of the antenna, the field created by the supplementary field in the dielectric, and the field created by the exciting aperture. The first of them represents an approximation usually used at the present time.^{2,3,4} Because it explains the character of the directional pattern in its principal features, certain simplifications can be introduced into the remaining terms, with confidence that the directional pattern will be changed little on account of that. Let us assume that the distribution function over the cross section of the antenna of all three fields entering Eq. (4) will be identical and agree with the distribution of the field of the characteristic wave:

$$\vec{E}_\tau(x', y') = \frac{1}{a} \vec{E}_0(x', y'), \tag{5}$$

$$\vec{E}'(x', y') = \vec{E}_\tau f'(z'). \tag{6}$$

If we substitute in (4) Eq. (5) and (6) and also the expressions for \vec{E}_1 and \vec{H}_1 , which in the distant zone have the form

$$\vec{E}_1 = -\vec{e}_x j \frac{60\pi}{\lambda r} e^{-jkr}, \tag{7}$$

$$\vec{H}_1 = \vec{e}_\varphi j \frac{1}{\lambda r} e^{-jkr}, \tag{8}$$

and also

$$r(x, y, z) = r(x, y) - z \cos \Theta,$$

after several transformations we obtain for the directional pattern the expression

$$F(\Theta) = F_0(\Theta) [F_1(\Theta) + F_2(\Theta) + F_3(\Theta)], \tag{9}$$

where

$$F_1(\Theta) = \pi N(\epsilon' - 1) a e^{j\psi} \frac{\sin \alpha}{\alpha} e^{-j\alpha}, \quad (10)$$

$$F_2(\Theta) = -j \frac{\cos \Theta}{2}, \quad (11)$$

$$F_3(\Theta) = \pi N(\epsilon' - 1) \frac{1}{L} \int_0^L f'(z') e^{jkz' \cos \Theta} dz', \quad (12)$$

$$F_0(\Theta) = \int_{S_T} E_0(x', y') e^{-jkr(x', y')} dx' dy', \quad (13)$$

$$\alpha = \pi N(\xi - \cos \Theta), \quad (14)$$

$$N = \frac{L}{\lambda}, \quad (15)$$

$$\xi = \frac{k_a}{k} = \frac{c}{v_f} \quad (16)$$

v_f is the phase velocity of the characteristic wave of the dielectric waveguide.

In order not to encumber the calculations too much we disregarded the influence of the ideally conducting screen here. Its role will be explained below.

In expression (9) the function $F_0(\Theta)$ is a multiplier of the element which was investigated by Fradin² for a cylindrical rod, and for a thin-walled dielectric tube with the diameter D has the form

$$F_0(\Theta) = \cos \left(\frac{kD}{2} \sin \Theta \right). \quad (17)$$

In both cases it represents a function of the angle Θ which gradually varies within the limits of the major lobe and the first minor lobes.

In the multiplier of the element in brackets in (9) the second and third terms represent supplementary terms for expressing the directional pattern of a first approximation of the type $\sin \alpha / \alpha$.

Let us deal with investigation of their influence in more detail.

The Influence of Direct Radiation of the Exciting Junction

If only that supplementary factor is considered, for the directional pattern with respect to power we obtain the following expression after several transformations⁵

$$\Psi^2(\Theta) = F_1'^2(\Theta) + \frac{1}{\pi N(\epsilon' - 1)a} F_1'(\Theta) \cos \Theta \cos \left(\psi - a + \frac{\pi}{2} \right), \quad (18)$$

where

$$F_1'(\Theta) = \frac{\sin \alpha}{\alpha}. \quad (19)$$

It follows from Eq. (18) that at sufficiently small values of a the influence of the second term can be perceptible, especially in the region of the first minor lobes of the pattern. In that case, depending on the angle ψ , either increase or decrease of the level of the minor lobes is possible. If we establish a definite value of the angle ψ (by including at the beginning of the antenna a small section with a different phase velocity), we can substantially lower the level of the minor lobes of tubular antennas.^{5, 6}

Let us examine the coefficient a in more detail. We will express it by two values characterizing the exciting junction and the dielectric waveguide: ρ_1 is the power transmission coefficient of the exciting junction of the antenna (the effectiveness of the excitation), a method of experimental determination of which was given previously,⁶ and

$$\rho_2 = \frac{W_i}{W_a},$$

where W_i and W_a are the fractions of power spreading in and outside the dielectric respectively. The latter value is found for a round rod in Fradin.² If the distribution of the field over the cross section is considered to be uniform and it also is assumed that the wave resistance of the dielectric waveguide is equal to the wave resistance of a vacuum (cf. Fradin,² p. 529) and equal to the amplitude ratio of the tangential components of the electric and magnetic fields on the exciting aperture, and then it can be found elementary arguments that

$$a = \sqrt{\frac{\rho_1 \rho_2}{\rho_1 + \rho_2}}. \quad (20)$$

For dielectric antennas used in practice, with $\epsilon' = 2.5$, the value of ρ_1 is in the range of from 0.5 (for tubes) to 0.85 (for rods).⁷ For round rods ρ_2 has a value of 0.7 to 1 (Fradin,² p. 514). The concentration of power in dielectric tubes can be judged by the numerical results of Unger,⁸ where the damping of the characteristic wave HE_{11} in tubes was found for various values of the ratio of the internal and external radii, including also the case of a continuous rod. One can conclude from those results that for tubes with $\epsilon' = 2.5$ whose wall thickness is 0.1 - 0.2 of the radius, the value of ρ_2 is of the order of 0.1 - 0.2. For such antennas a will have a value of 0.2 - 0.3.

If one takes into consideration the cited estimates of the value of a and formula (18), one can conclude that for tubular antennas the influence of direct radiation of the exciting junction can considerably change the directional pattern in the region of the minor lobes. That influence will be insignificant for rod antennas.

The Influence of the Supplementary Field in the Region of the Exciting Junction

It can be assumed that the supplementary field is localized in the vicinity of the exciting junction, where the characteristic wave of the antenna forms, and decreases with increase of the distance z ; to some extent it is analogous to a close field which forms in the direct proximity of heterogeneities in closed waveguides. No data are available on the character of that field. Only in Bobrovnikov's and Smironov's work⁹ was the field of a magnetic flux close to a wire over an impedance surface examined, and its damping character was confirmed there. To make clear the qualitative influence of that field on the directional pattern we will approximate the law of its distribution along the Z -axis with the expression

$$f'(z') = be^{-\beta z'} - jk_1 z' \quad (21)$$

If we neglect the influence of direct radiation of the exciting transition, then after uncomplicated transformations we obtain for the square of the array factor of expression (9)

$$\Psi_2^2(\Theta) = \left(\frac{\sin \alpha}{\alpha} \right)^2 + \frac{b}{a} e^{-\beta L/2} \frac{\operatorname{ch}^2 \beta \sin^2 \alpha_1 + \operatorname{sh}^2 \beta \cos \alpha_1}{\alpha_1^2 + \beta_2}$$

$$\cos \left[\psi + \alpha_1 - \alpha + \operatorname{arc} \operatorname{tg} \frac{\beta}{\alpha_1} - \operatorname{arc} \operatorname{tg}(\operatorname{th} \beta \operatorname{cth} \alpha_1) \right], \quad (22)$$

where

$$\alpha_1 = \pi N \left(\frac{k_1}{k} - \cos \Theta \right).$$

Here the second term, expressing the influence of the supplementary field, depends on its amplitude and rate of decay. It introduces substantial changes in the region of the minor lobes. Its influence can explain the absence of zeros in the directional patterns of real antennas. For tubular antennas that influence will be insignificant on account of the low concentration of the field in the dielectric. It will be most substantial for short and thick rod antennas. It is known from Fradin² that in that case a very substantial divergence is observed between experiment and calculations based on the model of a linear traveling-wave antenna.

It should be noted that the qualitative conclusions do not change if one adopts a law of the type of $be^{-\beta z'}$ instead of (21). A more precise analysis of the influence of the supplementary field is impossible at the present time, as no more detailed theoretical or experimental information about its character is available.

The Influence of Processes at the End of the Antenna

In relation to the characteristic wave of a dielectric waveguide the end of the antenna is heterogeneous. The reflection coefficient obtained for it is small,^{2,10} and its influence on the directional pattern ought to be expressed mainly in the form of reverse radiation, which is not observed. Therefore, its influence can be considered to be insignificant.

The Influence of an Ideally Conducting Screen

If we take \vec{E}_1 and \vec{H}_1 in the form of (7) and (8) we have neglected the influence of the screen. With consideration of it, instead of (7) it is necessary to write

$$\vec{E}_1 = -\vec{e}_x \frac{60\pi}{\lambda r} \left(e^{jkz \cos \Theta} - e^{-jkz \cos \Theta} \right). \quad (23)$$

Then in the array factor of expression (9) one must add the term

$$F_4 = -e^{-j\alpha_2} \frac{\sin \alpha_2}{\alpha_2}, \quad (24)$$

where

$$\alpha_2 = \pi N(\xi + \cos \Theta), \quad (25)$$

and also the corresponding additional terms to $F_2(\Theta)$, which are obtained by the replacement of α by α_2 in those terms. Term (24) will exert a basic influence on the array factor. Its role can be estimated qualitatively by making use of a generalized directional pattern of a linear traveling-wave antenna (Figure 2). On that graph the real directional pattern occupies the region from

$$\alpha_{\min} = \pi N(\xi - 1),$$

($\Theta = 0^\circ$) to

$$\alpha_{\max} = \pi N(\xi + 1).$$

($\Theta = 180^\circ$) and can be obtained from Figure 2 by graphical constructions.⁵ The term F_4 occupies the region from α_{\max} (which corresponds to $\Theta = 0^\circ$) to $\alpha_1(\Theta = 90^\circ)$ and influences mainly the most distant minor lobes.

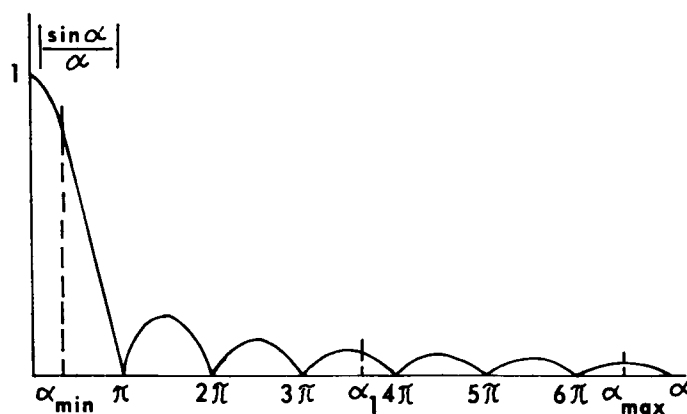


Figure 2

For an antenna without a screen, instead of its influence it is necessary to take into consideration the field created by the currents passing over the external surface of the exciting metallic waveguide. It can be expected that that influence will be perceptible only in the region of the most distant minor lobes.

Conical Dielectric Antennas

For approximate analysis of the properties of a conical antenna one can use an expression obtained by Sengupta¹¹ for the directional pattern of a linear traveling-wave antenna whose propagation constant varies linearly and fairly slowly along the axis of the antenna

$$F^2(\Theta) = \left(\frac{\sin \alpha}{\alpha} \right)^2 + \left[\frac{1}{4} \frac{\Delta k_a}{k_{av}} \left(1 + \frac{2\pi N}{\alpha} \right) \frac{\cos \alpha}{\alpha} \right]^2, \quad (26)$$

where

$$\alpha = \pi N (\xi_{av} - \cos \Theta),$$

$$k_{av} = \frac{k_1 + k_2}{2},$$

$$\Delta k_a = k_1 - k_2,$$

and k_1 and k_2 are the propagation constants at the beginning and end of the antenna.

Let us draw a graphic interpretation of that formula, using generalized directional patterns. On Figure 3 are curves 1 and 2 corresponding to the first and second terms of expression (26). The second term does not change the absolute level of the first minor lobe. If the relative antenna length is selected in accordance with the condition of obtaining a maximum amplification factor for an antenna homogeneous along its length, for which $k_a = k_{av}$ ¹²

$$\frac{k_{av}}{k} = 1 + \frac{1}{2N}, \quad (27)$$

then that corresponds to $\alpha_{\min} = \pi/2$ and the directional pattern of such an antenna will have no advantages. However, the antenna parameters are so selected that a lowering of the level of the minor lobes can be obtained by increasing the absolute level of the major lobe. This fact can be considered the main advantage of conical antennas.

Conclusion

The analysis of the influence of supplementary factors on the directional

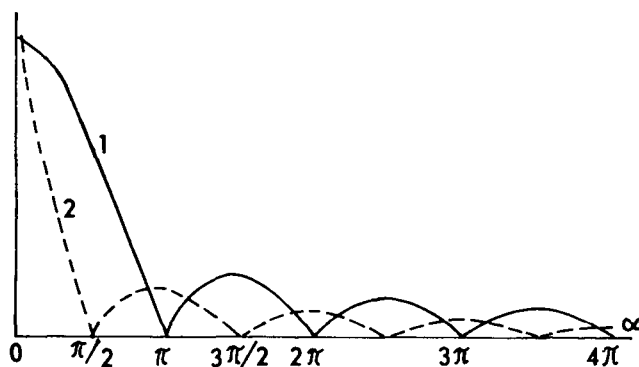


Figure 3

pattern of a dielectric antenna that has been made and was represented in first approximation in the form of (19) shows that the properties of the excited transition have a substantial influence on the directional pattern only of fairly short antennas. For long antennas, among which one can include piecewise linear antennas,¹³ antennas with modulation of the dielectric constant^{14, 16} and also long thin tubes with a spiral exciter,¹⁶ that influence will have a negligible value.

The examination was conducted by means of a number of parameters (a , ψ , b , and β) characterizing the field in an antenna. Precise determination of them will become possible only when the problems of excitation of dielectric rods and tubes with a wave HE_{11} have been solved and the character of the field in the region of the exciting junction has been investigated.

LITERATURE CITED

1. Rankis, G. Zh., "Reduction of the Problem of Finding the Field in a Dielectric Antenna to an Internal Problem of Electrodynamics," Uchenyye zapiski Rzhskogo politekhnich. in-ta (Scientific Notes of Riga Polytechnic Institute), Riga, 1962, 7, 3, 85.
2. Fradin, A. Z., Antenny sverkhvysokikh chastot (Ultrahigh-Frequency Antennas), Soviet Radio Publishing House, 1957.
3. Ayzenberg, G. Z., Antenny ul'trakorotkikh voln (Ultrashort-Wave Antennas), Svyaz'izdat, 1957.
4. Kiely, D. G., Dielectric Aerials, London, 1953.
5. Rankis, G. Zh., "The Question of the Influence of the Conditions of Excitation on the Directional Properties of Dielectric Antennas," Uchenyye zapiski Rzhskogo politekhnich. in-ta, Riga, 1963, 10, 1, 51.
6. Rankis, G. Zh., "The Parameters of Excitation of Dielectric Waveguides and Their Experimental Determination," Uchenyye zapiski Rzhskogo politekhnich. in-ta, Riga, 1963, 10, 1, 39.
7. Rankis, G. Zh., Issledovaniye dielektricheskikh antenn (An Investigation of Dielectric Antennas), Candidate's Dissertation, Leningrad Institute of Electrical Engineering imeni V. I. Ul'yanov (Lenin), 1963.
8. Unger, H. G., "Dielektrische Rohre als Wellenleiter." Archiew der elektrischen Ubertragung, 1954, 8, 6, 241.
9. Bobrovnikov, M. S. and Smirnov, V. P., "The Field in the Zone of a Source During Concentrated Excitation of an Impedance Surface," Izv. vuzov SSSR - Radiotekhnika, 1962, 5, 3, 321.
10. Rankis, G. Zh., "The Present Status of the Theory of Dielectric Antennas," Uchenyye zapiski Rzhskogo politekhnich. in-ta, Riga, 1960, 3, 1, 123.
11. Sengupta, D. L., "On Uniform and Linearly Tapered long Yagi Antennas," IRE Trans. on Antennas and Propagation, 1960, AP-8, 1, 11.
12. Hansen, W. W. and Woodyard, L. R., "A New Principle in Directional Antenna Design," Proceedings of the IRE, 1938, 26, 3, 333.

13. Trentini, G., "Uber Formgebung dielektrischer Riehtsstrahler," NTZ, 1957, 2, 60.
14. Thomas, A. S. and Zucker, F. J., "Radiation from Modulated Surface Wave Structures," IRE Nat. Conv. Rec., 1957, 1, 1953.
15. Pease, R. L., "Radiation from Modulated Surface Wave Structures," IRE Nat. Conv. Rec., 1957, 1, 161.
16. Ikrath, K. and Schneider, W., "Antenna Innovation. Glass Fiber Tube Focuses Microwave Beam," Electronics, 1962, 32, 38, 44.

UNCLASSIFIED

Security Classification

DOCUMENT CONTROL DATA - R & D		
(Security classification of title, body of abstract and indexing annotation must be entered when the overall report is classified)		
1. ORIGINATING ACTIVITY (Corporate author) Redstone Scientific Information Center Research and Development Directorate U. S. Army Missile Command Redstone Arsenal, Alabama 35809		2a. REPORT SECURITY CLASSIFICATION Unclassified
3. REPORT TITLE THE PRINCIPAL FACTORS DETERMINING THE DIRECTIONAL PATTERN OF A DIELECTRIC ANTENNA Izvestiya VUZOV SSSR-Radiotekhnika, 9, No. 1, 97-104 (1966).		2b. GROUP N/A
4. DESCRIPTIVE NOTES (Type of report and inclusive dates) Translated from the Russian		
5. AUTHOR(S) (First name, middle initial, last name) G. Zh. Rankis		
6. REPORT DATE 3 July 1967	7a. TOTAL NO. OF PAGES 12	7b. NO. OF REFS 16
8a. CONTRACT OR GRANT NO. N/A	9a. ORIGINATOR'S REPORT NUMBER(S) RSIC-686	
b. PROJECT NO. N/A	9b. OTHER REPORT NO(S) (Any other numbers that may be assigned this report)	
c. d.	AD	
10. DISTRIBUTION STATEMENT Distribution of this document is unlimited.		
11. SUPPLEMENTARY NOTES None	12. SPONSORING MILITARY ACTIVITY Same as No. 1	
13. ABSTRACT The directional pattern of a dielectric antenna is analyzed on the basis of integral equations. Additional factors are established which determine the difference of the directivity pattern of a real antenna from an idealized linear travelling-wave antenna: direct radiation of the exciting junction, a supplementary field in the region of the exciting junction, etc. Estimates of the magnitude of their influence were obtained for different varieties of dielectric antennas. The properties of conical dielectric antennas are briefly examined.		

DD FORM 1473

REPLACES DD FORM 1473, 1 JAN 64, WHICH IS OBSOLETE FOR ARMY USE.

UNCLASSIFIED
Security Classification

14.	KEY WORDS	LINK A		LINK B		LINK C	
		ROLE	WT	ROLE	WT	ROLE	WT
	Dielectric antenna Characteristic wave Infinite dielectric waveguide Integral equations Directional pattern Exciting junction						

(U) DISTRIBUTION

	No. of Copies		No. of Copies
<u>EXTERNAL</u>		U. S. Atomic Energy Commission	1
Air University Library	1	ATTN: Reports Library, Room G-017	
ATTN: AUL3T		Washington, D. C. 20545	
Maxwell Air Force Base, Alabama 36112		U. S. Naval Research Laboratory	1
U. S. Army Electronics Proving Ground	1	ATTN: Code 2027	
ATTN: Technical Library		Washington, D. C. 20390	
Fort Huachuca, Arizona 85613		Weapons Systems Evaluation Group	1
U. S. Naval Ordnance Test Station	1	Washington, D. C. 20305	
ATTN: Technical Library, Code 753		John F. Kennedy Space Center, NASA	2
China Lake, California 93555		ATTN: KSC Library, Documents Section	
U. S. Naval Ordnance Laboratory	1	Kennedy Space Center, Florida 32899	
ATTN: Library		APGC (PGBPS-12)	1
Corona, California 91720		Eglin Air Force Base, Florida 32542	
Lawrence Radiation Laboratory	1	U. S. Army CDC Infantry Agency	1
ATTN: Technical Information Division		Fort Benning, Georgia 31905	
P. O. Box 808		Argonne National Laboratory	1
Livermore, California 94550		ATTN: Report Section	
Sandia Corporation	1	9700 South Cass Avenue	
ATTN: Technical Library		Argonne, Illinois 60440	
P. O. Box 969		U. S. Army Weapons Command	1
Livermore, California 94551		ATTN: AMSWE-RDR	
U. S. Naval Postgraduate School	1	Rock Island, Illinois 61201	
ATTN: Library		Rock Island Arsenal	1
Monterey, California 93940		ATTN: SWERI-RDI	
Electronic Warfare Laboratory, USAECOM	1	Rock Island, Illinois 61201	
Post Office Box 205		U. S. Army Cmd. & General Staff College	1
Mountain View, California 94042		ATTN: Acquisitions, Library Division	
Jet Propulsion Laboratory	2	Fort Leavenworth, Kansas 66027	
ATTN: Library (TDS)		Combined Arms Group, USACDC	1
4800 Oak Grove Drive		ATTN: Op. Res., P and P Div.	
Pasadena, California 91103		Fort Leavenworth, Kansas 66027	
U. S. Naval Missile Center	1	U. S. Army CDC Armor Agency	1
ATTN: Technical Library, Code N3022		Fort Knox, Kentucky 40121	
Point Mugu, California 93041		Michoud Assembly Facility, NASA	1
U. S. Army Air Defense Command	1	ATTN: Library, I-MICH-OSD	
ATTN: ADSX		P. O. Box 29300	
Ent Air Force Base, Colorado 80912		New Orleans, Louisiana 70129	
Central Intelligence Agency	4	Aberdeen Proving Ground	1
ATTN: OCR/DD-Standard Distribution		ATTN: Technical Library, Bldg. 313	
Washington, D. C. 20505		Aberdeen Proving Ground, Maryland 21005	
Harry Diamond Laboratories	1	NASA Sci. & Tech. Information Facility	5
ATTN: Library		ATTN: Acquisitions Branch (S-AK/DL)	
Washington, D. C. 20438		P. O. Box 33	
Scientific & Tech. Information Div., NASA	1	College Park, Maryland 20740	
ATTN: ATS		U. S. Army Edgewood Arsenal	1
Washington, D. C. 20546		ATTN: Librarian, Tech. Info. Div.	
		Edgewood Arsenal, Maryland 21010	

	No. of Copies		No. of Copies
National Security Agency ATTN: C3/TDL Fort Meade, Maryland 20755	1	Brookhaven National Laboratory Technical Information Division ATTN: Classified Documents Group Upton, Long Island, New York 11973	1
Goddard Space Flight Center, NASA ATTN: Library, Documents Section Greenbelt, Maryland 20771	1	Watervliet Arsenal ATTN: SWEWV-RD Watervliet, New York 12189	1
U. S. Naval Propellant Plant ATTN: Technical Library Indian Head, Maryland 20640	1	U. S. Army Research Office (ARO-D) ATTN: CRD-AA-IP Box CM, Duke Station Durham, North Carolina 27706	1
U. S. Naval Ordnance Laboratory ATTN: Librarian, Eva Liberman Silver Spring, Maryland 20910	1	Lewis Research Center, NASA ATTN: Library 21000 Brookpark Road Cleveland, Ohio 44135	1
Air Force Cambridge Research Labs. L. G. Hanscom Field ATTN: CRMCLR/Stop 29 Bedford, Massachusetts 01730	1	Systems Engineering Group (RTD) ATTN: SEPIR Wright-Patterson Air Force Base, Ohio 45433	1
Springfield Armory ATTN: SWESP-RE Springfield, Massachusetts 01101	1	U. S. Army Artillery & Missile School ATTN: Guided Missile Department Fort Sill, Oklahoma 73503	1
U. S. Army Materials Research Agency ATTN: AMXMR-ATL Watertown, Massachusetts 02172	1	U. S. Army CDC Artillery Agency ATTN: Library Fort Sill, Oklahoma 73504	1
Strategic Air Command (OAI) Offutt Air Force Base, Nebraska 68113	1	U. S. Army War College ATTN: Library Carlisle Barracks, Pennsylvania 17013	1
Picatinny Arsenal, USAMUCOM ATTN: SMUPA-VA6 Dover, New Jersey 07801	1	U. S. Naval Air Development Center ATTN: Technical Library Johnsville, Warminster, Pennsylvania 18974	1
U. S. Army Electronics Command ATTN: AMSEL-CB Fort Monmouth, New Jersey 07703	1	Frankford Arsenal ATTN: C-2500-Library Philadelphia, Pennsylvania 19137	1
Sandia Corporation ATTN: Technical Library P. O. Box 5800 Albuquerque, New Mexico 87115	1	Div. of Technical Information Ext., USAEC P. O. Box 62 Oak Ridge, Tennessee 37830	1
ORA(RRRT) Holloman Air Force Base, New Mexico 88330	1	Oak Ridge National Laboratory ATTN: Central Files P. O. Box X Oak Ridge, Tennessee 37830	1
Los Alamos Scientific Laboratory ATTN: Report Library P. O. Box 1663 Los Alamos, New Mexico 87544	1	Air Defense Agency, USACDC ATTN: Library Fort Bliss, Texas 79916	1
White Sands Missile Range ATTN: Technical Library White Sands, New Mexico 88002	1	U. S. Army Air Defense School ATTN: AKBAAS-DR-R Fort Bliss, Texas 79906	1
Rome Air Development Center (EMLAL-1) ATTN: Documents Library Griffiss Air Force Base, New York 13440	1		

	No. of Copies		No. of Copies
U. S. Army CDC Nuclear Group Fort Bliss, Texas 79916	1	<u>INTERNAL</u>	
Manned Spacecraft Center, NASA ATTN: Technical Library, Code BM6 Houston, Texas 77058	1	Headquarters U. S. Army Missile Command Redstone Arsenal, Alabama ATTN: AMSMI-D	1
Defense Documentation Center Cameron Station Alexandria, Virginia 22314	20	AMSMI-XE, Mr. Lowers	1
		AMSMI-XS, Dr. Carter	1
		AMSMI-Y	1
		AMSMI-R, Mr. McDaniel	1
		AMSMI-RAP	1
U. S. Army Research Office ATTN: STINFO Division 3045 Columbia Pike Arlington, Virginia 22204	1	AMSMI-RBLD	10
		USACDC-LnO	1
		AMSMI-RB, Mr. Croxton	1
		AMSMI-RBT	8
U. S. Naval Weapons Laboratory ATTN: Technical Library Dahlgren, Virginia 22448	1	National Aeronautics & Space Administration Marshall Space Flight Center ATTN: MS-T, Mr. Wiggins	5
U. S. Army Engineer Res. & Dev. Labs. ATTN: Scientific & Technical Info. Br. Fort Belvoir, Virginia 22060	2	Huntsville, Alabama	
Langley Research Center, NASA ATTN: Library, MS-185 Hampton, Virginia 23365	1		
Research Analysis Corporation ATTN: Library McLean, Virginia 22101	1		
U. S. Army Tank Automotive Center ATTN: SMOTA-RIS.1 Warren, Michigan 48090	1		
Hughes Aircraft Company Electronic Properties Information Center Florence Ave. & Teale St. Culver City, California 90230	1		
Atomics International, Div. of NAA Liquid Metals Information Center P. O. Box 309 Canoga Park, California 91305	1		
Foreign Technology Division ATTN: Library Wright-Patterson Air Force Base, Ohio 45400	1		
Clearinghouse for Federal Scientific and Technical Information U. S. Department of Commerce Springfield, Virginia 22151	1		
Foreign Science & Technology Center, USAMC ATTN: Mr. Shapiro Washington, D. C. 20315	3		
National Aeronautics & Space Administration Code USS-T (Translation Section) Washington, D. C. 20546	2		